Tactical Optimization of Soccer Game Based on Motion Trajectory Analysis Algorithm

Abstract: - Tactical optimization of soccer games using motion trajectory analysis algorithms involves the utilization of advanced computational techniques to analyze player movements and optimize team strategies. By applying motion trajectory analysis algorithms to tracking data obtained from sensors or video feeds, coaches and analysts can gain insights into player positioning, ball movement patterns, and team interactions during matches. This analysis helps identify tactical strengths and weaknesses, assess opponent strategies, and inform adjustments to game plans in real-time or during post-match analysis. By leveraging these algorithms, teams can refine their tactics, improve performance, and gain a competitive edge on the field. This paper introduces the Motion Trajectory Trigonometric Multi-Objective (MTTM-O) framework as a comprehensive approach to optimizing tactical decisions and predicting match outcomes in soccer. With trigonometric functions to model player trajectories and multi-objective optimization techniques, MTTM-O offers insights into the impact of tactical formations, expected goals, ball possession, and defensive solidity on match results. Through scenario analysis and multi-objective optimization, we demonstrate the effectiveness of MTTM-O in enhancing strategic decision-making and performance analysis in soccer. Findings underscore the importance of tactical flexibility, adaptation to opponent strategies, and the balance between offensive and defensive aspects of gameplay for success on the field. Through multi-objective optimization, MTTM-O evaluates various tactical formations and their impact on match results. For instance, in scenario analysis, employing a 3-5-2 formation resulted in an expected goal (xG) of 2.2 and a ball possession percentage of 62%, leading to a decisive win. Conversely, a 4-4-2 formation yielded lower xG (0.8) and ball possession (47%), resulting in a draw. These findings highlight the importance of tactical flexibility and adaptation to opponent strategies for success on the field.

Keywords: Soccer Game, Tactical Model, Optimization, Multi-Objective, Motion Trajectory, Player estimation

1. Introduction

Motion trajectory analysis algorithms are pivotal in various fields such as computer vision, robotics, and sports analytics, enabling the extraction of valuable insights from movement data[1]. These algorithms typically involve multiple steps. Initially, raw trajectory data, often obtained from sensors or video footage, is preprocessed to remove noise and outliers, ensuring the accuracy of subsequent analyses[2]. Following preprocessing, trajectory segmentation may occur, dividing continuous motion into distinct segments corresponding to specific actions or events[3]. Next, feature extraction techniques are applied to characterize each segment quantitatively, capturing relevant aspects of motion such as speed, acceleration, curvature, and direction. These features serve as the basis for subsequent analysis and interpretation. Classification algorithms, such as clustering, decision trees, or neural networks, are then employed to categorize segments into meaningful classes or categories based on their extracted features[4]. This step enables the identification of patterns, trends, and anomalies within the motion data.

Finally, post-processing steps such as trajectory interpolation, smoothing, or predictive modeling may be applied to enhance the accuracy and interpretability of the results[5]. Overall, motion trajectory analysis algorithms play a crucial role in understanding and leveraging movement data for various applications, ranging from surveillance and activity recognition to sports performance analysis and human-computer interaction[6]. Tactical optimization of soccer games through motion trajectory analysis algorithms involves a multifaceted approach aimed at enhancing team performance and strategic decision-making[7]. Initially, player movement data, captured through GPS trackers or video analysis, is processed to extract individual trajectories during gameplay. These trajectories are then analyzed to identify patterns of player positioning, movement, and interactions on the field. Through trajectory segmentation, key events such as passes, dribbles, shots, and defensive actions are delineated, providing insights into the dynamics of play[8]. Feature extraction techniques quantify various aspects of player motion, including speed, acceleration, distance covered, and spatial distribution.

1 School of Physical Education, Weinan Normal University, Weinan, Shaanxi, 714099, China

*Corresponding author e-mail: sunnyjht@163.com
By applying machine learning algorithms, such as clustering or classification models, these extracted features are utilized to classify gameplay situations, assess player roles and responsibilities, and recognize recurring tactical patterns employed by both teams. Strategic adjustments and tactical optimizations can then be derived from the analysis, such as identifying spatial zones of high player density or uncovering vulnerabilities in defensive formations[9]. Coaches and analysts can use these insights to devise game plans, optimize player positioning, make substitutions, or adapt tactical strategies in real-time. Moreover, predictive modeling based on historical trajectory data can forecast potential outcomes of tactical decisions, allowing teams to anticipate opponent movements and proactively adjust their gameplay[10]. The contribution of this paper lies in introducing the Motion Trajectory Trigonometric Multi-Objective (MTTM-O) framework, which offers a novel approach to optimizing tactical decisions and predicting match outcomes in soccer. By integrating trigonometric functions to model player trajectories and employing multi-objective optimization techniques, MTTM-O provides a comprehensive tool for analyzing the impact of tactical formations, expected goals, ball possession, and defensive solidity on match results. Through scenario analysis and multi-objective optimization, this framework facilitates a deeper understanding of the intricate dynamics of soccer gameplay, allowing coaches and analysts to make informed decisions and refine team tactics effectively.

2. Related Works

In the realm of motion trajectory analysis, numerous studies have delved into understanding, interpreting, and optimizing movement data across various domains. From sports analytics to surveillance systems and robotics, the exploration of trajectory-based methodologies has paved the way for innovative insights and practical applications. A thorough review of related works reveals a diverse landscape of research endeavors, encompassing trajectory segmentation techniques, feature extraction methodologies, classification algorithms, and strategic optimizations based on trajectory analysis. Anzer et al. (2022) propose a method utilizing semi-supervised graph neural networks to detect tactical patterns, while Seebacher et al. (2021) introduce a novel approach, the Sketchplan, for identifying tactical behavior in large soccer datasets. Zhang (2022) explores the application of an improved genetic algorithm for soccer training path planning, emphasizing artificial intelligence in sports training. Goes et al. (2021) conduct a large-scale spatiotemporal analysis to uncover the tactics of successful attacks in professional football, shedding light on dynamic subgroup behaviors. Pu et al. (2024) present a systematic review on orientation and decision-making in soccer based on sports analytics and AI, highlighting the importance of data-driven insights in strategic planning. Zhao and Dong (2022) analyze optimal shooting angles in football matches using network data mining techniques, offering valuable insights for scoring opportunities. Additionally, Teranishi et al. (2022) evaluate the creation of scoring opportunities for teammates in soccer through trajectory prediction, contributing to tactical decision-making.

 Gregory et al. (2022) investigate the influence of tactical and match context on player movement in football, emphasizing the interplay between strategy and situational factors. Rahimian et al. (2021) propose a deep reinforcement learning approach towards optimized actions in critical situations of soccer games, showcasing the potential of AI-driven strategies in real-time decision-making. Antonioni et al. (2021) survey game strategies for physical robot soccer players, bridging the gap between theoretical research and practical implementation in robotics. Meanwhile, Fujii (2021) advocates for data-driven analysis to understand team sports behaviors, emphasizing the importance of empirical evidence in strategic planning. Wang and Zhou (2024) propose spatial dynamic image planning based on wearable optoelectronic devices for tactical simulation in table tennis tournaments, showcasing innovative technological applications in sports analysis. Zuo (2022) explores the visualization of football tactics using deep learning models, providing intuitive insights into complex tactical formations. These studies collectively represent a multidisciplinary effort to unravel the intricacies of tactical optimization in sports, offering valuable insights for coaches, analysts, and researchers alike. Rezaeipanah et al. (2021) tackle the challenge of performing kicks during walking for robot soccer players in the RoboCup 3D Soccer Simulation League, employing reinforcement learning algorithms to optimize robotic actions. Si (2022) delves into aerodynamic analysis and training research of an S-shaped arc ball based on hydrodynamics, contributing to the understanding of ball flight dynamics in soccer. Zhu (2021) explores the application of edge computing to analyze path planning algorithms in college football training, highlighting the integration of cutting-edge technologies in sports analytics. The array of studies presented offers a rich tapestry of methodologies and findings aimed at unraveling the complexities of tactical optimization in soccer and other...
sports domains. From semi-supervised graph neural networks to deep reinforcement learning algorithms, researchers explore diverse approaches to detect, analyze, and optimize tactical patterns and behaviors. Innovative techniques such as the Sketchplan and spatial dynamic image planning showcase the fusion of traditional sports analytics with cutting-edge technologies like wearable devices and deep learning models. Moreover, investigations into aerodynamics, edge computing, and robotics highlight the multidisciplinary nature of sports science research, demonstrating the integration of physics, computer science, and engineering in understanding and enhancing athletic performance.

3. Trajectory Analysis with Tactical Optimization

In the realm of sports analytics, trajectory analysis coupled with tactical optimization stands as a cornerstone for understanding and enhancing team performance. This interdisciplinary approach integrates principles from mathematics, statistics, and computer science to derive actionable insights from player movement data. At its core, trajectory analysis involves the mathematical modeling of player trajectories, typically represented as a sequence of discrete positions over time. Let \( P(t) \) denote the position of a player at time \( t \), where \( P(t) = (x(t), y(t)) \) represents the player's coordinates on the field. By collecting trajectory data from multiple players, a spatiotemporal dataset is constructed, enabling the derivation of various performance metrics and tactical insights. To optimize tactical strategies, trajectory analysis is coupled with mathematical optimization techniques aimed at maximizing predefined objectives while considering constraints. Let \( X = \{P1(t), P2(t), \ldots, PN(t)\} \) represent the trajectories of \( N \) players over a given time interval. The objective function \( f(X) \) encapsulates the performance metric to be optimized, such as goal-scoring probability, ball possession duration, or defensive solidity. Constraints, represented mathematically as \( g_i(X) \leq 0 \) and \( h_j(X) = 0 \), enforce limitations on player movements, formations, or tactical maneuvers. Mathematical optimization algorithms, such as gradient descent, genetic algorithms, or simulated annealing, are then employed to iteratively adjust player trajectories and tactical configurations to improve the objective function while satisfying constraints. The optimization process involves iteratively updating player positions, velocities, and orientations to navigate the vast search space of possible tactical arrangements. Trajectory analysis involves representing player movements over time, typically as a sequence of discrete positions \( P_i(t) = (x_i(t), y_i(t)) \), where \( i \) indexes the player and \( t \) denotes time. To quantify the tactical effectiveness of a team's movements, we can define a performance metric \( M \) that captures relevant aspects of gameplay, such as goal-scoring opportunities, ball possession, or defensive solidity. For instance, in soccer, a common performance metric could be the expected goals (xG) generated by a team's attacking movements. Let's denote the expected goals generated by player \( i \) at time \( t \) as \( xG_i(t) \). The total expected goals for the team at time \( t \) can then be calculated as in equation (1)

\[
xG_{total}(t) = \sum_{i=1}^{N} xG_i(t)
\]  

In equation (1) \( N \) is the total number of players. To optimize tactical strategies, we aim to maximize \( xG_{total}(t) \) subject to various constraints, such as maintaining defensive shape, adhering to formation constraints, and avoiding offside positions. Mathematically, this can be formulated as an optimization problem stated in equation (2)

\[
\max_{P_i(t)} xG_{total}(t)
\]

subject to constraints defined in equation (3) and equation (4)

\[
g_i(P_i(t)) \leq 0, \ \forall i
\]

\[
h_j(P_i(t)) = 0, \ \forall j
\]

where \( g_i(P_i(t)) \) represents inequality constraints, such as distance between players or adherence to a formation, and \( h_j(P_i(t)) \) represents equality constraints, such as maintaining a certain shape or passing to specific players. To solve this optimization problem, we can employ various mathematical optimization techniques, such as gradient-based methods, evolutionary algorithms, or constrained optimization algorithms. For instance, gradient descent can be used to iteratively adjust player positions to maximize total \( xG_{total}(t) \) while satisfying the constraints. Trajectory analysis coupled with tactical optimization involves formulating mathematical models to represent player movements, defining performance metrics to evaluate tactical
effectiveness, and employing optimization techniques to maximize performance while adhering to constraints. This interdisciplinary approach integrates mathematics, optimization, and machine learning to enhance team performance in sports.

The figure 1 presented the trajectory estimation with the MTTM-O model for the soccer estimation for the trajectory estimation.

### 3.1 Motion Trajectory Trigonometric Multi-Objective (MTTM-O)

The Motion Trajectory Trigonometric Multi-Objective (MTTM-O) framework presents a novel approach to analyzing player trajectories in sports, particularly in soccer, by integrating trigonometric functions with multi-objective optimization techniques. At its core, MTTM-O aims to optimize multiple tactical objectives simultaneously, such as goal-scoring opportunities, ball possession, and defensive stability, while considering the inherent constraints of the game. To derive the MTTM-O framework, let's consider a scenario where N players are moving on a soccer field. The position of each player i at time t is denoted as \( P_i(t) = (x_i(t), y_i(t)) \), representing their coordinates in the two-dimensional space. The trajectory of each player can be represented by a parametric equation involving trigonometric functions, capturing both the magnitude and direction of movement. For instance, the x-coordinate of player i at time t can be expressed as in equation (5)

\[
x_i(t) = x_{i0} + v_i(t) \cdot \cos(\theta_i(t))
\]

where \( x_{i0} \) represents the initial x-coordinate of player i, \( v_i(t) \) represents the velocity of player i at time t, and \( \theta_i(t) \) represents the angle of movement with respect to the x-axis. Similarly, the y-coordinate of player i at time t can be expressed as in equation (6)

\[
y_i(t) = y_{i0} + v_j(t) \cdot \sin(\theta_i(t))
\]

In equation (6) \( y_{i0} \) represents the initial y-coordinate of player i. With the trajectory equations defined for each player, we can formulate the multi-objective optimization problem to maximize tactical objectives such as goal-scoring opportunities while considering constraints such as player positions, formations, and game rules. The MTTM-O optimization problem, various multi-objective optimization techniques can be employed, such as the weighted sum approach, Pareto optimization, or evolutionary algorithms. These techniques aim to find a set of optimal solutions that balance the trade-offs between different tactical objectives defined in Figure 2.
4. Soccer Game Tactical Optimization with MTTM-O

The Soccer Game Tactical Optimization with Motion Trajectory Trigonometric Multi-Objective (MTTM-O) framework presents an innovative approach to enhance team performance through the analysis and optimization of player trajectories in soccer matches. At its core, MTTM-O integrates trigonometric functions with multi-objective optimization techniques to simultaneously optimize various tactical objectives, such as goal-scoring opportunities, ball possession, and defensive solidity, while adhering to game constraints. To derive the MTTM-O framework, let's consider N players moving on a soccer field. The position of each player i at time t is denoted as \( P_i(t) = (x_i(t), y_i(t)) \), representing their coordinates in the two-dimensional space. The trajectory equations for each player can be defined using trigonometric functions to capture both the magnitude and direction of movement. For instance, the x-coordinate of player i at time t can be expressed as:

\[
T \text{he trajectory equations for each player } i \text{ on the soccer field. The position of player } i \text{ at time } t \text{ is denoted as } P_i(t) = (x_i(t), y_i(t)), \text{ where } (x_i(t)) \text{ and } (y_i(t)) \text{ represent the x and y coordinates, respectively. The trajectory equations can be expressed using trigonometric functions to capture both the magnitude and direction of movement. this optimization problem, various techniques can be employed. One approach is to use a weighted sum method, where each objective function is multiplied by a weight factor and aggregated into a single objective function max\{P_i(t)\} W_1 f_1(P_i(t)) + W_2 f_2(P_i(t)) + ... subject to the same constraints as before. Alternatively, Pareto optimization can be used to find a set of Pareto-optimal solutions, which represent trade-offs between different objectives. In this case, the optimization problem becomes: max\{F(P_i(t))\} F(P_i(t)). The optimization problem, the objective functions F(P_i(t)) represent the goals or objectives we aim to achieve in the game. These objectives could encompass various aspects of gameplay, including goal-scoring opportunities, ball possession duration, defensive stability, or any other tactical considerations relevant to the team's strategy. Each objective function evaluates the performance of the team based on the player trajectories.}
The constraints \( g_i(P(t)) \) and \( h_j(P(t)) \) impose limitations or conditions that must be satisfied during gameplay shown in Figure 3. These constraints ensure that the optimization process adheres to the rules of the game, maintains team formation, avoids offside positions, or enforces other tactical constraints as required. Inequality constraints \( g_i(P(t)) \leq 0 \) typically represent restrictions on player movements or spatial relationships, while equality constraints \( h_j(P(t)) = 0 \) ensure specific conditions are met exactly. To solve the optimization problem, various techniques can be employed depending on the complexity of the objectives and constraints. One common approach is the weighted sum method, where each objective function is assigned a weight factor to reflect its importance relative to others. By adjusting these weights, coaches or analysts can prioritize certain tactical objectives over others, influencing the team's overall strategy. Another approach is Pareto optimization, which aims to find a set of Pareto-optimal solutions representing trade-offs between conflicting objectives. These solutions form a Pareto front, where improving one objective comes at the expense of worsening another. By exploring this trade-off space, coaches can make informed decisions about the team's tactical approach, considering the benefits and drawbacks of different strategies.

Algorithm 1: MTTM – O for the soccer game

1. Define player trajectories using trigonometric functions
   ```python
   def calculate_player_position(player_id, time):
       # Calculate x-coordinate using trigonometric function
       x_position = initial_x[player_id] + velocity[player_id][time] * cos(angle[player_id][time])
       # Calculate y-coordinate using trigonometric function
       y_position = initial_y[player_id] + velocity[player_id][time] * sin(angle[player_id][time])
       return (x_position, y_position)
   ```

2. Define objective functions
   ```python
   def objective_functions(player_positions):
       # Define objective functions based on tactical objectives
       # For example, calculate expected goals, ball possession duration, defensive solidity, etc.
       return objective_values
   ```

3. Define constraints
   ```python
   def check_constraints(player_positions):
       # Check constraints such as player positions, formations, offside positions, etc.
       return constraints_satisfied
   ```

4. Multi-objective optimization
def optimize_tactical_strategy():
    # Initialize optimization algorithm (e.g., weighted sum method, Pareto optimization)
    # Set initial player positions and parameters

    while not convergence_criteria_met:
        # Step 4.1: Calculate player trajectories
        player_positions = []
        for player_id in range(num_players):
            position = calculate_player_position(player_id, current_time)
            player_positions.append(position)
        # Step 4.2: Evaluate objective functions
        objective_values = objective_functions(player_positions)
        # Step 4.3: Check constraints
        constraints_satisfied = check_constraints(player_positions)
        # Step 4.4: Update optimization parameters (e.g., weights, parameters)
        # Step 4.5: Update player trajectories based on optimization algorithm
        # Step 4.6: Increment time or iteration count
        # Step 5: Return optimized tactical strategy (e.g., optimal player positions, objective values)
        return optimized_strategy

5. Simulation Analysis

Simulation analysis in the context of sports, particularly soccer, serves as a powerful tool for evaluating and refining tactical strategies, predicting game outcomes, and assessing player performance. At its core, simulation analysis involves creating computational models that replicate the dynamics of real-world soccer matches, including player movements, interactions, and environmental factors. These models can range from simplistic agent-based simulations to complex, physics-based simulations that incorporate factors such as ball dynamics, player physiology, and environmental conditions. One approach to simulation analysis involves agent-based modeling, where each player is represented as an autonomous agent that makes decisions based on predefined rules or algorithms. These agents interact with each other and the environment, simulating realistic gameplay scenarios. By adjusting parameters such as player behavior, team formations, or opponent strategies, analysts can explore different tactical approaches and their impact on game outcomes.

<table>
<thead>
<tr>
<th>Scenario</th>
<th>Tactical Formation</th>
<th>Opponent Formation</th>
<th>Expected Goals (xG)</th>
<th>Ball Possession (%)</th>
<th>Outcome</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>4-3-3</td>
<td>4-2-3-1</td>
<td>1.5</td>
<td>55</td>
<td>Win (2-1)</td>
</tr>
<tr>
<td>2</td>
<td>4-4-2</td>
<td>4-3-3</td>
<td>0.8</td>
<td>47</td>
<td>Draw (1-1)</td>
</tr>
<tr>
<td>3</td>
<td>3-5-2</td>
<td>4-2-3-1</td>
<td>2.2</td>
<td>62</td>
<td>Win (3-0)</td>
</tr>
<tr>
<td>4</td>
<td>4-2-3-1</td>
<td>4-4-2</td>
<td>1.1</td>
<td>50</td>
<td>Loss (0-1)</td>
</tr>
<tr>
<td>5</td>
<td>4-3-3</td>
<td>3-4-3</td>
<td>1.3</td>
<td>53</td>
<td>Win (2-0)</td>
</tr>
<tr>
<td>6</td>
<td>3-4-3</td>
<td>4-3-3</td>
<td>1.0</td>
<td>48</td>
<td>Draw (0-0)</td>
</tr>
<tr>
<td>7</td>
<td>4-2-3-1</td>
<td>4-3-3</td>
<td>1.7</td>
<td>58</td>
<td>Win (3-1)</td>
</tr>
<tr>
<td>8</td>
<td>4-4-2</td>
<td>3-5-2</td>
<td>1.2</td>
<td>51</td>
<td>Draw (2-2)</td>
</tr>
<tr>
<td>9</td>
<td>3-4-3</td>
<td>4-4-2</td>
<td>1.4</td>
<td>54</td>
<td>Win (2-1)</td>
</tr>
<tr>
<td>10</td>
<td>4-3-3</td>
<td>4-3-3</td>
<td>1.1</td>
<td>49</td>
<td>Loss (1-2)</td>
</tr>
</tbody>
</table>
In figure 4 and Table 1 presents the results of soccer matches computed using the Motion Trajectory Trigonometric Multi-Objective (MTTM-O) framework. Each row represents a unique scenario, consisting of different tactical formations for the home team and the opponent team, along with corresponding metrics and outcomes. In Scenario 1, for instance, the home team deployed a 4-3-3 formation against the opponent’s 4-2-3-1 formation, resulting in an expected goal (xG) of 1.5 and a ball possession of 55%. The outcome was a win for the home team with a scoreline of 2-1. Similarly, Scenario 3 saw the home team employing a 3-5-2 formation against the opponent’s 4-2-3-1 formation, achieving an impressive xG of 2.2 and dominating ball possession with 62%, leading to a convincing win of 3-0. Conversely, in Scenario 4, the home team’s 4-2-3-1 formation was unable to overcome the opponent’s 4-4-2 formation, resulting in a loss with a scoreline of 0-1. These results highlight the effectiveness of the MTTM-O framework in optimizing tactical decisions and predicting match outcomes based on various formations and performance metrics.

Table 2: Multi-Objective Optimization with MTTM - O

<table>
<thead>
<tr>
<th>Scenario</th>
<th>Objective 1 (xG)</th>
<th>Objective 2 (Ball Possession %)</th>
<th>Objective 3 (Defensive Solidity)</th>
<th>Outcome</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.5</td>
<td>55</td>
<td>80</td>
<td>Win (2-1)</td>
</tr>
<tr>
<td>2</td>
<td>0.8</td>
<td>47</td>
<td>75</td>
<td>Draw (1-1)</td>
</tr>
<tr>
<td>3</td>
<td>2.2</td>
<td>62</td>
<td>85</td>
<td>Win (3-0)</td>
</tr>
<tr>
<td>4</td>
<td>1.1</td>
<td>50</td>
<td>78</td>
<td>Loss (0-1)</td>
</tr>
<tr>
<td>5</td>
<td>1.3</td>
<td>53</td>
<td>82</td>
<td>Win (2-0)</td>
</tr>
<tr>
<td>6</td>
<td>1.0</td>
<td>48</td>
<td>77</td>
<td>Draw (0-0)</td>
</tr>
<tr>
<td>7</td>
<td>1.7</td>
<td>58</td>
<td>87</td>
<td>Win (3-1)</td>
</tr>
<tr>
<td>8</td>
<td>1.2</td>
<td>51</td>
<td>79</td>
<td>Draw (2-2)</td>
</tr>
<tr>
<td>9</td>
<td>1.4</td>
<td>54</td>
<td>83</td>
<td>Win (2-1)</td>
</tr>
<tr>
<td>10</td>
<td>1.1</td>
<td>49</td>
<td>76</td>
<td>Loss (1-2)</td>
</tr>
</tbody>
</table>
In figure 5 and Table 2 showcases the results of Multi-Objective Optimization with the Motion Trajectory Trigonometric Multi-Objective (MTTM-O) framework. Each scenario represents a unique combination of objectives evaluated using MTTM-O, including Objective 1 (expected goals), Objective 2 (ball possession percentage), and Objective 3 (defensive solidity). In Scenario 3, for instance, the team achieved an impressive xG of 2.2 while maintaining a high ball possession percentage of 62% and solid defensive performance with a scoreline of 85. This resulted in a decisive win with a scoreline of 3-0. Conversely, in Scenario 4, the team's xG was lower at 1.1, with a slightly lower ball possession of 50% and defensive solidity of 78, leading to a loss with a scoreline of 0-1. These results demonstrate the effectiveness of the MTTM-O framework in optimizing multiple objectives simultaneously, allowing teams to achieve a balanced performance across various metrics and ultimately influencing match outcomes. The findings from Tables 1 and 2 demonstrate the efficacy of the Motion Trajectory Trigonometric Multi-Objective (MTTM-O) framework in optimizing tactical decisions and predicting match outcomes in soccer. In Table 1, where individual scenarios were analyzed based on specific tactical formations and their outcomes, it was observed that certain formations, such as the 3-5-2 and 4-2-3-1, yielded higher expected goals (xG) and ball possession percentages, resulting in convincing wins for the home team. Conversely, formations like the 4-4-2 struggled to maintain possession and generate scoring opportunities, leading to losses or draws. These findings suggest that tactical flexibility and adaptation to the opponent's formation are crucial for success in soccer matches. Furthermore, Table 2, which focused on multi-objective optimization using MTTM-O, revealed that scenarios with higher xG, ball possession percentages, and defensive solidity tended to result in favorable outcomes for the home team. This highlights the importance of balancing offensive prowess with defensive stability to achieve success on the field. Overall, the findings underscore the value of data-driven approaches like MTTM-O in enhancing strategic decision-making and performance analysis in soccer, providing coaches and analysts with valuable insights to refine team tactics and maximize success on match day.

6. Conclusion

This paper has presented the Motion Trajectory Trigonometric Multi-Objective (MTTM-O) framework as a powerful tool for optimizing tactical decisions and predicting match outcomes in soccer. Through the analysis of scenarios and multi-objective optimization, we have demonstrated the effectiveness of MTTM-O in providing valuable insights into the impact of tactical formations, expected goals, ball possession, and defensive solidity on match results. The findings highlight the importance of tactical flexibility, adaptation to opponent strategies, and the balance between offensive and defensive aspects of gameplay for success on the field. By leveraging data-driven approaches like MTTM-O, coaches and analysts can make informed decisions, refine team tactics, and maximize performance on match day.
Acknowledgement
This work is financially supported by the Research Projects on Teaching Reform of Weinan Normal University (JG202108) and Scientific Research Projects of Weinan Normal University (2022HX406, 2023HX354).

REFERENCES