

PTS techniques assessment for improving PAPR reduction in LTE and Advanced LTE

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Abstract— Due to advancement in age and growing demands, there has been a rapid evolution in the field of communication. Hence, single carrier waves are being replaced by multi-carrier systems like Orthogonal Frequency Division Multiplexing (OFDM) and Generalized Frequency Division Multiplexing (GFDM) which are nowadays being implemented commonly. In the OFDM system, orthogonally placed subcarriers are used to carry the data from the transmitter to the receiver end. The presence of guard band in these systems deals with the problem of intersymbol interference (ISI) and noise is minimized by the larger number of subcarriers. However, the large Peak to Average Power Ratio (PAPR) of these signals has undesirable effects on the system. In this work, we will focus on the GFDM systems as well as methods that reduce the PAPR issue to improve the efficiency.

Index Terms—GFDM, ISI, MIMO, OFDM, PAPR, PTS.

1. INTRODUCTION

The successful deployment of killer applications in wireless communication technology has allowed its rapid development in the past 20 years with major impact on modern life and way the societies operate in politics, economy, education, entertainment, logistics & travel, and industry. The evolution of wireless communication systems technologies can be discretely grouped into various generations based on the level of maturity of the underlying technology. The classification into generations is not standardized on any given metrics or parameters and as such does not represent a severe demarcation. However, it represents a perspective which is commonly agreed upon, both by industry and academia, and hence conceived to be an unwritten standard [1]. The LTE (Long Term Evolution) and LTE-Advanced are the latest mobile communications standards developed by the Third Generation Partnership Project (3GPP).

GFDM for Generalized Frequency Division Multiplexing [1] is a multicarrier modulation technique which can be foreseen as a potential alternative for upcoming wireless networks. GFDM attractive features include reduced low Peak-to-Average Ratio (PAPR), which is the crucial shortcomings of Orthogonal Frequency Division Multiplexing (OFDM) used in present day wireless communication networks.

High PAPR causes severe degradation of Bit Error Rate (BER) performance and in-band and out-of-band distortion occurs in the non-linear amplifier and leads to power inefficiency in the Radio Frequency (RF) section of the transmitter.

There are different techniques for PAPR reduction [3], [4] including Selective Mapping (SLM) [5], Tone Reservation (TR) [6], Clipping and Filtering [7] and Partial Transmit Sequence (PTS) [8],[9]. PTS is considered to be one of the best techniques to reduce the PAPR in GFDM systems.

2. GFDM SYSTEMS

Generalized Frequency Division Multiplexing (GFDM) is a candidate waveform that has been investigated as a component in the physical layer (PHY) of future wireless communication systems. Particularly, GFDM can use Time-Frequency Localization (TFL) of the transmit signal to address spectral agility and aggregation of carriers with an adaptation of the prototype filter and resource grid. However, inherent self-interference between subcarriers of GFDM hinders the application of standard spatial multiplexing (SM) detection algorithms.

A data source provides the binary data vector \vec{b} , which is encoded to obtain \vec{b}_c . A mapper, e.g. QAM Modulation, maps the encoded bits to symbols from a 2^μ -valued complex constellation where μ is the modulation order. The resulting vector \vec{d} denotes a data block that contains N elements, which can be decomposed into K subcarriers with M subsymbols each according to $\vec{d}_c = (\vec{d}_0^T, \dots, \vec{d}_{M-1}^T)^T$ and $\vec{d}_m = (d_{0,m}, \dots, d_{k-1,m})^T$. The total number of symbols follows as $N = KM$. The individual elements $d_{k,m}$ correspond to the data transmitted on the k_{th} subcarrier and in the m_{th} subsymbol of the block. The details of the GFDM modulator are shown in equation (1). Each $d_{k,m}$ is transmitted with the corresponding pulse shape:

$$g_{k,m}[n] = g[(n - mK) \bmod N] \exp\left[-j2\pi \frac{k}{K} n\right] \quad (1)$$

With n denoting the sampling index. Each $g_{k,m}[n]$ is a time and frequency shifted version of a prototype filter $g[n]$, where the module operation makes $g_{k,m}[n]$ a circularly shifted version of $g_{k,0}[n]$ and the complex exponential performs the shifting operation in frequency. The transmit samples $\vec{x} = (x[n])^T$ are obtained by superposition of all transmit symbols:

$$x[n] = \sum_{k=0}^{K-1} \sum_{m=0}^{M-1} g_{k,m}[n] d_{k,m}, n = 0, \dots, N-1 \quad (2)$$

Collecting the filter samples in a vector $\vec{g}_{k,m} = (g_{k,m}[n])^T$ allows to formulate Equation (2) as

$$\vec{x} = A\vec{d} \quad (3)$$

Where A is a $KM \times KM$ transmitter matrix with a structure according to:

$$A = (\vec{g}_{0,0}, \dots, \vec{g}_{k-1,0}, \vec{g}_{0,1}, \dots, \vec{g}_{k-1,m-1}) \quad (4)$$

As one can see, $\vec{g}_{1,0} = [A]_{n,2}$ and $\vec{g}_{0,1} = [A]_{n,K+1}$ are circularly frequency and time-shifted versions of, $\vec{g}_{0,0} = [A]_{n,1}$. At this point, \vec{x} contains the transmit samples that correspond to the GFDM data block \vec{d} . Lastly, on the transmitter side, a cyclic prefix of N_{CP} samples is added to produce \vec{x} .

A. Peak to Average Power Ratio (PAPR)

Due to the large number of sub-carriers in typical Multicarrier Modulation (MCM) systems, the amplitude of the transmitted signal has a large dynamic range, leading to in-band distortion and out-of-band radiation when the signal is passed through the nonlinear region of the power amplifier.

Peak Power is defined as:

$$\text{Max}[x(t) * x^*(t)] = \text{Max} \left[\sum_0^{k-1} a_k e^{\frac{j2\pi k t}{T}} \sum_0^{k-1} a_k^* e^{\frac{-j2\pi k t}{T}} \right] \quad (5)$$

Average power is as follows:

$$E[x(t)x^*(t)] = E \left[\sum_0^{k-1} a_k e^{\frac{j2\pi k t}{T}} \sum_0^{k-1} a_k^* e^{\frac{-j2\pi k t}{T}} \right] \quad (6)$$

So, mathematically PAPR is given by,

$$\text{PAPR} = \text{Max}[x(t)x^*(t)] / E[x(t)x^*(t)] \quad (7)$$

The Complementary Cumulative Distribution Functions CCDF formula that approximates the PAPR of a multicarrier signal with Nyquist sampling rate is derived from the central limit theorem [11] and is given by:

$$\text{CCDF}(\text{PAPR}_0) = 1 - (1 - e^{-x^2})^N \quad (8)$$

B. Solid-State Power Amplifier (SSPA)

The SSPA [12] shows non-linear characteristics, as it causes distortion of the signals, particularly high PAPR values. Consequently, the BER performance of the system is decreased. The Rapp model of Solid-State Power Amplifier (SSPA) is defined by following Amplitude-to-Amplitude Modulation (AM/AM) and Amplitude-to-Phase Modulation (AM/PM) characteristics:

$$V_{out} = \frac{V_{in}}{(1 + (|V_{in}|/U_{sat})^{2p})^{\frac{1}{2p}}} \quad (9)$$

Where p is the smoothness factor and U_{sat} is the output saturation level.

C. The Partial Transmit Sequence (PTS) technique

PTS scheme [8] is a common method to reduce PAPR of OFDM signal. Its basic principle can be described as follows:

Let X be an input symbol sequence as presented in Equation (10) :

$$X = [X_0, X_1, \dots, X_N] \quad (10)$$

This sequence is then partitioned into V "disjoint" symbol subsequences $\{X_v, v = 1, 2, \dots, V\}$ as in Equation (11):

$$X = \sum_{v=1}^V X_v \quad (11)$$

It introduces rotating vector: $\{a_v = e^{j\theta_v}, v = 1, 2, \dots, V; \theta_v \in [0, 2\pi]\}$ which is known as Side Information (SI), where each signal subsequence X_v is multiplied by a unit magnitude constant a_v , to generate that is given by Equation (12):

$$Y = \sum_{v=1}^V a_v X_v \quad (12)$$

One can get time-domain signal through IFFT, as expressed in Equation (13):

$$y = \text{IFFT}(Y) = \sum_{v=1}^V a_v X_v \quad (13)$$

PAPR value is then compared by selecting different phase factors, so as to yield the phase factor vector for OFDM signals with the minimum PAPR. The corresponding objective function can be written as in Equation (14):

$$[a_1, a_2, \dots, a_v] = \arg \min(\max \left| \sum_{v=1}^V a_v X_v \right|^2) \quad (14)$$

Where 'argmin' stands for the decision condition at the minimum value of the function. So PAPR performance of the GFDM system is improved through finding the best phase factor $\{a_v, v = 1, 2, \dots, V\}$ at the cost of $V-1$ times IFFT. Figure 1 shows a typical GFDM system with traditional PTS.

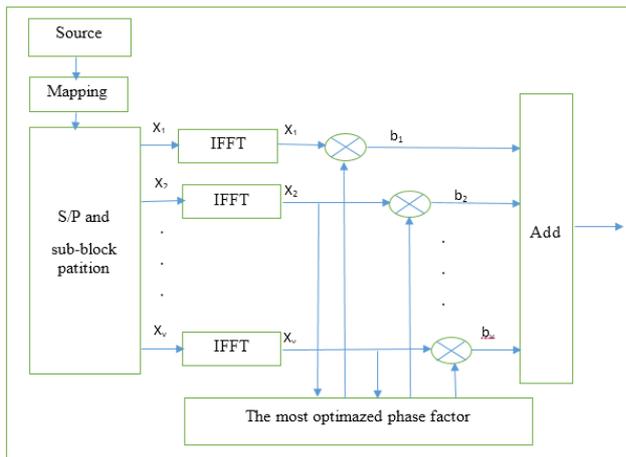


Fig 1. PTS method block.

3. DIFFERENT PTS TECHNIQUES

In the PAPR reduction process, PTS does not deteriorate the orthogonality of subcarriers but it needs lots of IFFTs and requires an exhaustive search over all combinations of allowed weighting coefficients, which brings a much higher computational load.

Several solutions have been proposed recently [17] to overcome this issue. Modified PTS technique is an effective way to cut down the computational complexity, however, the performance of PAPR is still a limitation, compared with the ordinary PTS technique. Modified PTS with the interleaving scheme is proposed by using interleaved sub-block partition and pulse shape technique to avoid multiple IFFT in PAPR reduction. Although this method reduces computational complexity, it does not improve well the PAPR performance.

In the present work, we will focus on two types of methods: Probabilities-PTS such as Optimal-PTS, Random Search PTS, and others, and Artificial PTS such as ABC-PTS and BFO-PTS which are based on artificial behavior.

A. Probabilities Algorithms

I. optimal-PTS

The Optimal PTS (O-PTS) [13] is a promising technique that can reduce the PAPR, while its complexity increases rapidly as the number of sub-blocks increases.

Let X denote a random input signal in frequency domain with length N . X is partitioned into V disjoint sub blocks $X=[X^0, X^1, X^2, \dots, X^{N-1}]^T$ which are then combined to minimize the PAPR in time domain. The sub block partition is based on interleaving in which the computational complexity is less compared to adjacent and Pseudo-random, however, it has the worst PAPR performance among them.

By applying the phase rotation factor $\mathbf{b}^v = e^{j\theta^v}$, $v=1,2,3, \dots, V$ to the IFFT of the v^{th} sub-block X_v , the time domain signal after combining is given by:

$$x'(b) = \sum_{v=1}^V b_v x_v \quad (15)$$

Where $x'(b)=[x'_0(b), x'_1(b), \dots, x'_{NL-1}(b)]^T$ and L is the over sampling factor. The objective is to find the optimum signal $x'(b)$ with lowest PAPR.

Both b and x can be shown in matrix form as follows:

$$b = \begin{bmatrix} b_1 & \dots & b_1 \\ \vdots & \vdots & \vdots \\ b_v & \dots & b_v \end{bmatrix}_{N \times V} \quad (16)$$

$$x = \begin{bmatrix} b_{1,0} & \dots & b_{1,NL-1} \\ \vdots & \vdots & \vdots \\ b_{v,0} & \dots & b_{v,NL-1} \end{bmatrix}_{NL-1 \times V} \quad (17)$$

It should be noted that all elements of each row of matrix b are of same values and this is in accordance with O-PTS method. In order to have exact PAPR calculation, at least 4 times oversampling is necessary. As oversampling of x , adds zeros to vector, hence number of phase sequence to multiply to matrix x will remain same. Now, the process is performed by choosing optimization parameter b' according to the following condition:

$$b' = \arg \min \left(\max_{0 \leq k \leq NL-1} \left| \sum_{v=1}^V b_v x_v \right| \right) \quad (18)$$

Once the optimum b' is found, the optimum signal is transmitted to the next block. Finding optimum b' , requires performing an exhaustive search for $(V-1)$ phase factors since one phase factor can remain fixed, $b_1=1$. Hence W^{V-1} iterations should be performed to find optimum phase factor, where W is the number of allowed phase factors.

II. Random Search (RS-PTS)

Random search algorithms [15] are useful for many global optimization problems with continuous and/or discrete variables. Typically random search algorithms sacrifice a guarantee of optimality for finding a good solution quickly with convergence results in probability. Random search algorithms include simulated annealing, genetic algorithms, evolutionary programming, particle swarm optimization, and colony optimization, to name a few.

A random search algorithm refers to an algorithm that uses some kind of randomness or probability (typically in the form of a pseudo-random number generator). This method may be called a Monte Carlo method or a stochastic algorithm in the literature. The term metaheuristic is also commonly associated with random search algorithms.

The problem of designing algorithms that obtain global optimal solutions is very difficult when there is no overriding structure that indicates whether a local solution is indeed a global one.

III. I-PTS

In this section, I-PTS algorithm for PAPR reduction is considered [14], as it is a problem of traversing the binary tree.

The solution of I-PTS is always updated for improvements purposes and hence is quickly trapped in a local optimum. Therefore, Instead of using the linear search of I-PTS, the Metropolis criterion is applied to decide the current phase factor $b = \{b_m; m=1,2,\dots,M\}$ is accepted or is rejected. This can be described within the following steps:

1 -Suppose that b' is the phase factor obtained from the previous search and $\Delta E = \text{PAPR}(b) - \text{PAPR}(b')$.

2-if $\Delta E \leq 0$, accept the move and keep the current b .

3-if $\Delta E > 0$, accept the move with probability $e^{\frac{-\Delta E}{TK}}$.
where $T_k = \alpha \cdot T_{k-1}; \alpha \in [0.8,1]$.

4- The phase factor which does not show the minimum PAPR may be chosen, thus the local optimum convergence can be avoided and the PAPR performance is improved consequently.

Moreover, due to the linear search of I-PTS, a different selection of initial phase factor may show diverse PAPR performance.

Another iteration PTS is to eliminate the effect of initial phase factor. The phase factor that is achieved by the previous iteration is set as the initial phase factor of the current search, thus the search is closer to the optimal phase factor. The optimum phase factor with minimum PAPR is then obtained after U times. The most important is to note is that more cyclic time provides the better performance but with higher complexity, hence an appropriate U should be chosen to obtain the good compromise between PAPR performance and complexity. The PTS algorithm should perform an exhaustive search for M phase factors, Consequently, $D = W^M$ sets of phase factors are searched to find the optimum set of phase factors. The search complexity increases exponentially with the number of sub-blocks M . I-PTS needs M sets of search to find the sub-optimum phase factors with much PAPR performance decline.

B. Artificial Algorithms

I. Artificial Bee Colony (ABC-PTS)

It was recently proposed by Karaboga [15].In the ABC algorithm, employed bees, onlooker bees, and scout bees are tasked with finding optimum food sources, and first, the food source positions are generated randomly. In the PAPR reduction problem, a food source position is equivalent to phase vector $b_i = [b_{i1}, b_{i2}, b_{i(V-1)}]$ where $i = 1, \dots, SN$, and SN denotes the population size, which is composed of the employed bees or the onlooker bees. The employed bees look for a new food source within the neighborhood of the previous source. If the nectar amount of the new source is higher than the previous one, the new source is memorized as a possible optimum solution. In the ABC-PTS, the new phase vector (the new food source) is expressed by

$$b'_i = b_i + \varphi_i(b_i - b_k) \quad (19)$$

where b_k is a solution within the neighborhood of b_i , and φ_i is a random number in the range of $[-1, 1]$. The nectar amount of the food source determines the quality or fitness of the solution that is expressed as:

$$fit(b_i) = \begin{cases} \frac{1}{1 + f(b_i)} & \text{iff}(b_i) \geq 0 \\ 1 + abs(f(b_i)) & \text{iff}(b_i) < 0 \end{cases} \quad (20)$$

where $f(b_i)$ represents the PAPR value of the signal and is desired to be at a minimum. The probability of an onlooker bee selecting a food source is calculated as:

$$p_i = \frac{fit(b_i)}{\sum_{i=1}^{SN} fit(b_i)} \quad (21)$$

After an onlooker bee reaches a food source, it looks for a new source within the neighborhood of the previous one and memorizes the food sources according to their fitness. After the employed bees and onlooker bees complete their searches, if the fitness values of the food sources do not improve with a number of iterations that is called the "limit" value, employed bees become the scout bees. The scout bees look for new food sources randomly by:

$$b_i = \min(b_i) + rand(0,1) * (\max(b_i) - \min(b_i)) \quad (22)$$

where $\min(b_i)$ and $\max(b_i)$ are the lower and upper bounds of the phase vector.

The above steps are repeated within in a cycle, called the maximum number of cycles (MCN). In a cycle, possible SN solutions are produced. In the ABC-PTS algorithm, $MCN * SN$ possible solutions are produced to find the optimum phase vector.

II. Bacterial Foraging Optimization (BFO-PTS)

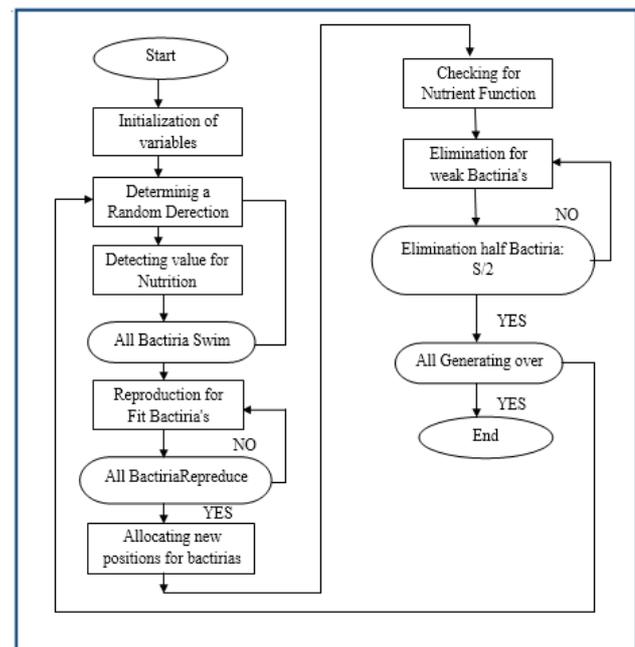


Fig 2.Flowchart of BFO

E. coli recently introduced the Bacterial Foraging Optimization algorithm (BFO)[16] for numerical optimization problems. The Flowchart of BFO shown in Figure 2.

4. Simulation Results

The Performance of GFDM was tested through computer simulation by setting the parameters as shown in Table 1.

TABLE I
GFDM PARAMETERS

Parameter	Notation	Value
Modulation	-	QAM 16
Samples per symbol	N	256
No. of active subcarriers	K	64
Block size(symbols)	M	256
Sampling frequency(MHz)	Fs	2
Symbol duration(μ s)	Ts	60
Block duration (μ s)	Tb	60
Channel model	-	AWGN, Rayleigh

A. PAPR Reduction

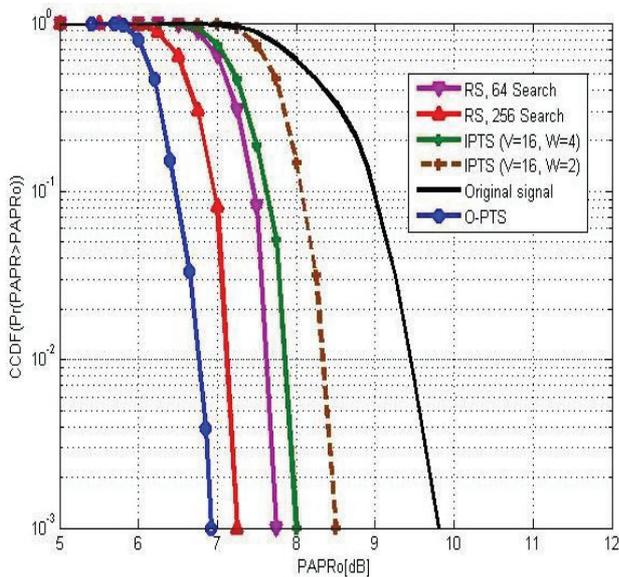


Fig 3. Comparison between probabilities algorithms

Figure 3 reveals that the best algorithm to reduce PAPR is O-PTS, but the problem of complexity and search number still remains. Random search algorithm also provides good results with only 256 search.

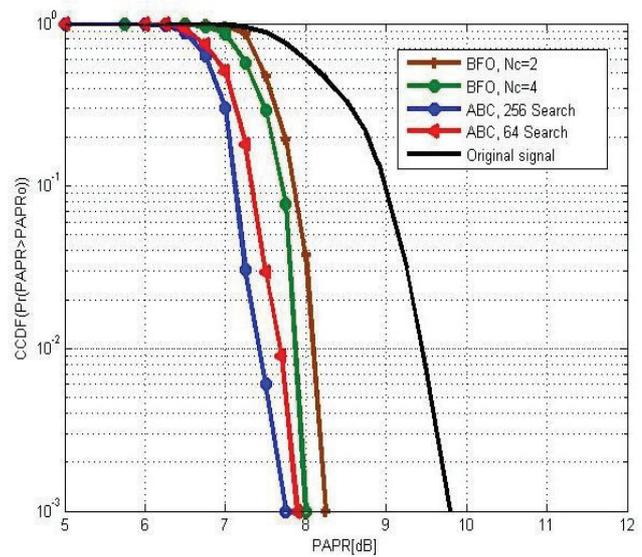


Fig 4. Comparison of PAPR performance (Nc = 2, 4, 6)

Figure 4 shows the PAPR reduction performance with a different number of chemotactic loop Nc.

As Nc increases, the PAPR performance of BFA-PTS has small improvement while the computational complexity becomes high accordingly. Therefore, an appropriate iteration number Nc=4 is the best choice to achieve the excellent PAPR reduction performance with very low complexity. Similarly, the variable PAPR performance caused by different swim length Ns, and the perfect swim length is chosen as Ns= 4.

B. BER Performance

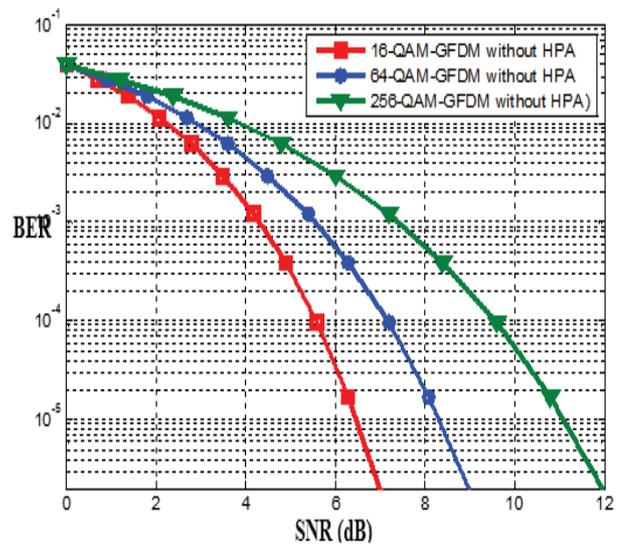


Fig 5. The Performance of GFDM without HPA in AWGN channel.

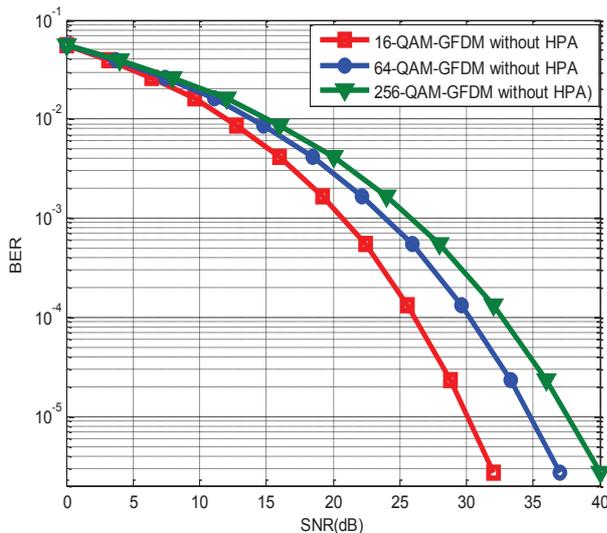


Fig 6. The Performance of GFDM without HPA in Rayleigh Fading channel.

Figures 5 and 6 represent the performance of GFDM system using different modulations: 16-QAM, 64-QAM and 256-QAM in a Gaussian channel and Rayleigh Fading channel without channel coding. We note that the results of the 16-QAM modulation are better than those obtained by the modulation 64QAM and 256-QAM. We can conclude that performance of the system decreases when the number of constellations increases.

Figures 7 and 8 represent the performance of GFDM system in the presence of SSPA model with a Gaussian channel (AWGN) and a multipath channel (Rayleigh Fading channel). We can note that the system is affected by the use of high power amplifier while the aim of this work is to reduce PAPR to improve the performance of the system. Simulation results show that the performance of the system decreases when the value of IBO decreases, which means the level of the saturation of the amplifier diminish.

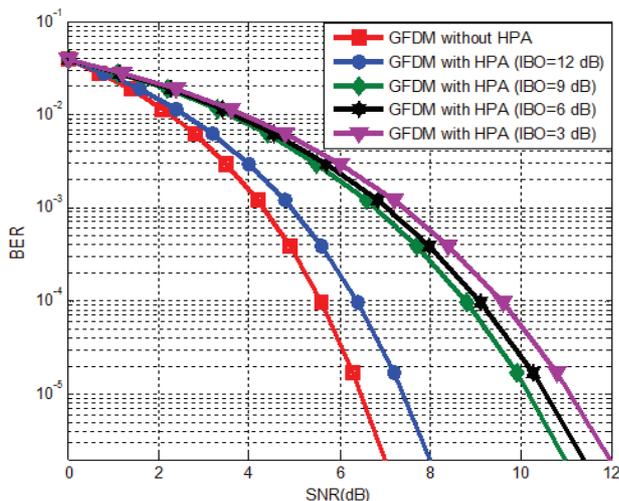


Fig 7. Performance of GFDM in the presence of SSPA in AWGN channel

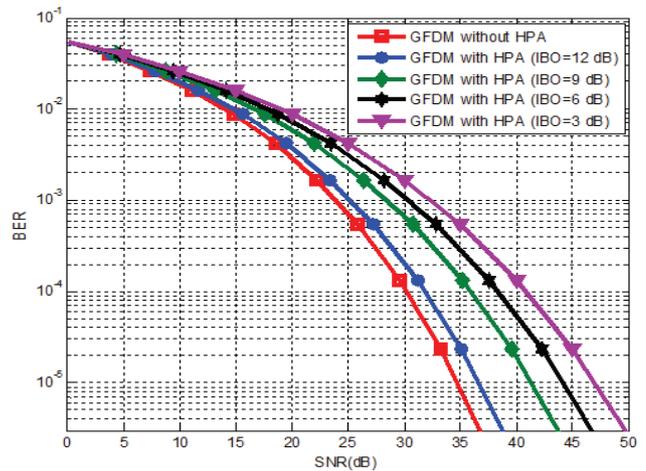


Fig 8. Performance of GFDM with HPA in Rayleigh Fading channel.

5. Conclusion

In this paper, almost all Partial Transmit Sequence (PTS) techniques for PAPR reduction in OFDM/GFDM systems are undertaken. Optimum-PTS technique is the preminent method for PAPR reduction while its drawback is optimization of Phase factor and complexity. Random-Search PTS is the best technique that makes use of random optimization and sub-block circular permutation which reduce the computational complexity and equivalently improve the performance for PAPR reduction.

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